

Bipolar Junction Transistors (BJT)

Transistors

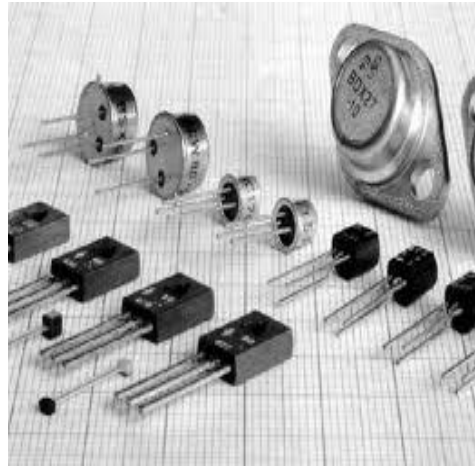
- Evolution of electronics
 - In need of a device that was small, robust, reliable, energy efficient and cheap to manufacture
- 1947
 - **John Bardeen, Walter Brattain and William Shockley** invented transistor
- Transistor Effect
 - “when electrical contacts were applied to a crystal of germanium, the output power was larger than the input.”



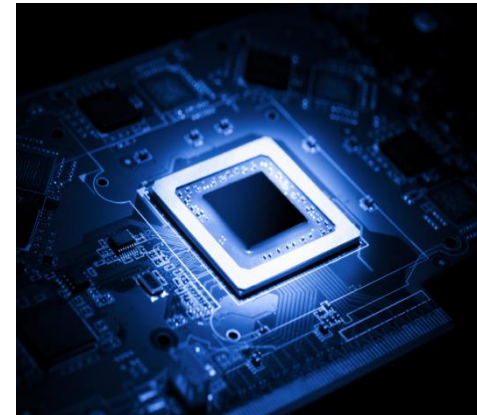
Transistors



First Transistor



Different types and sizes



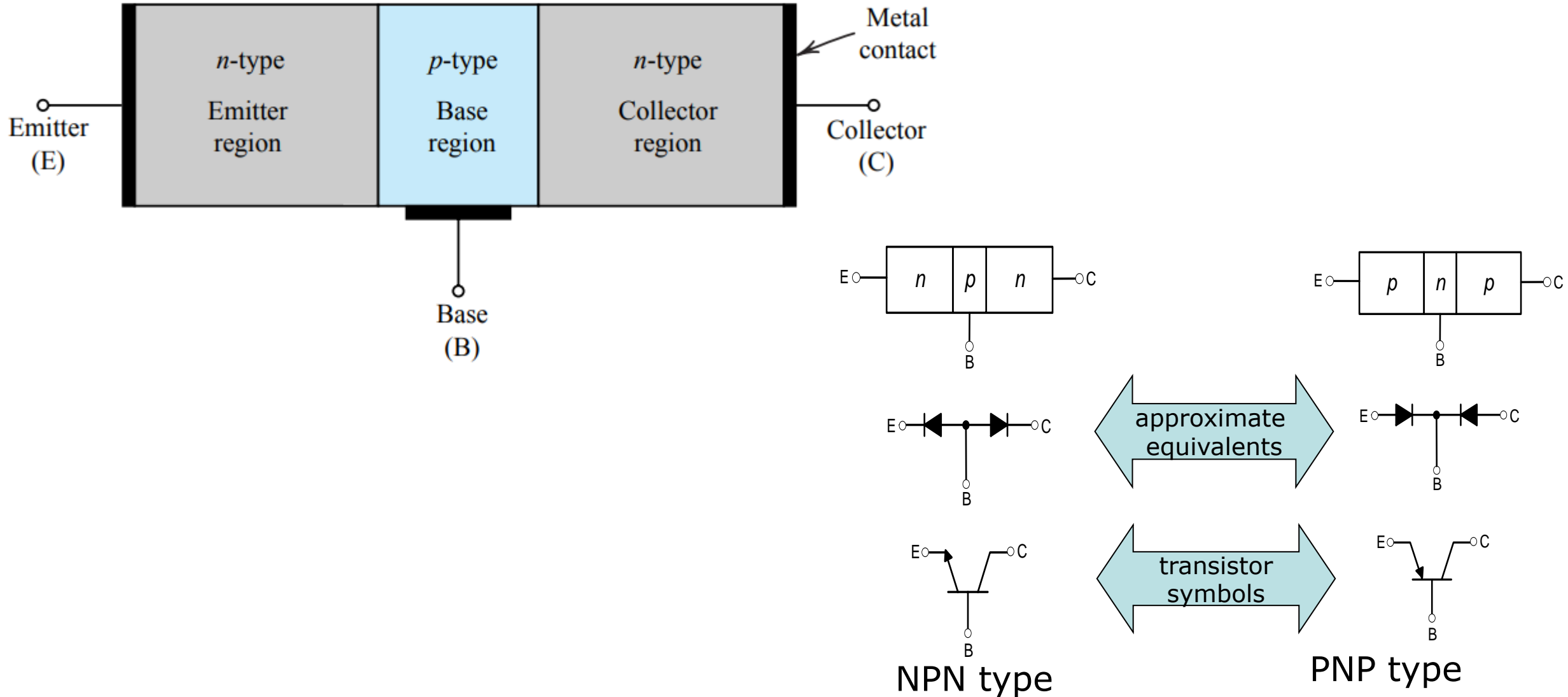
Modern Electronics

General Applications



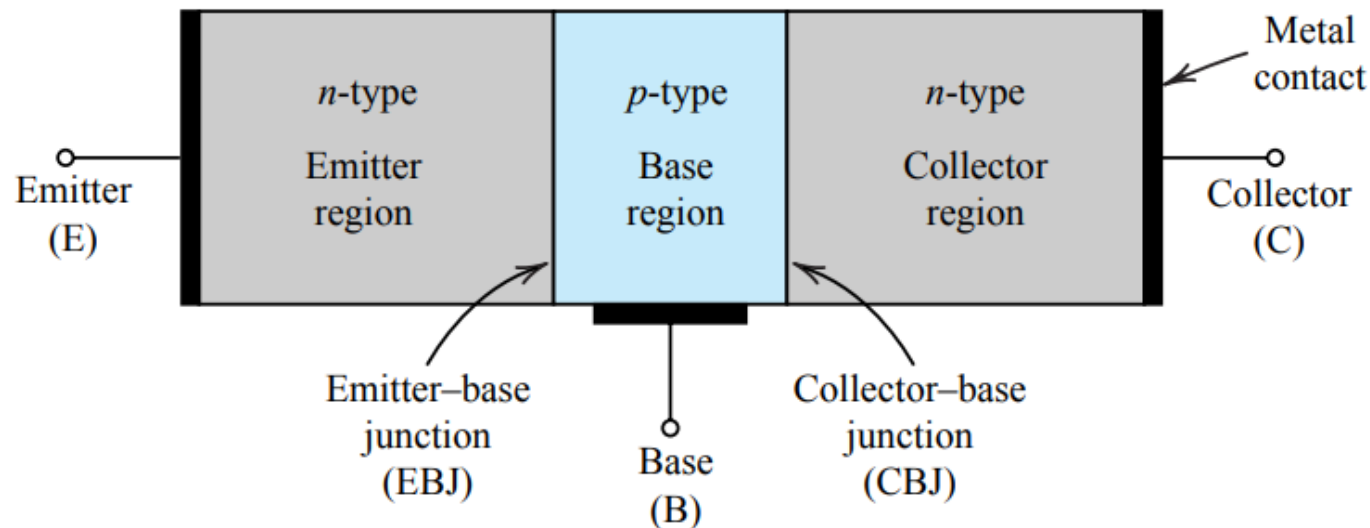
BJT Device Structure

- A transistor has three doped regions: **Emitter, Base, Collector**



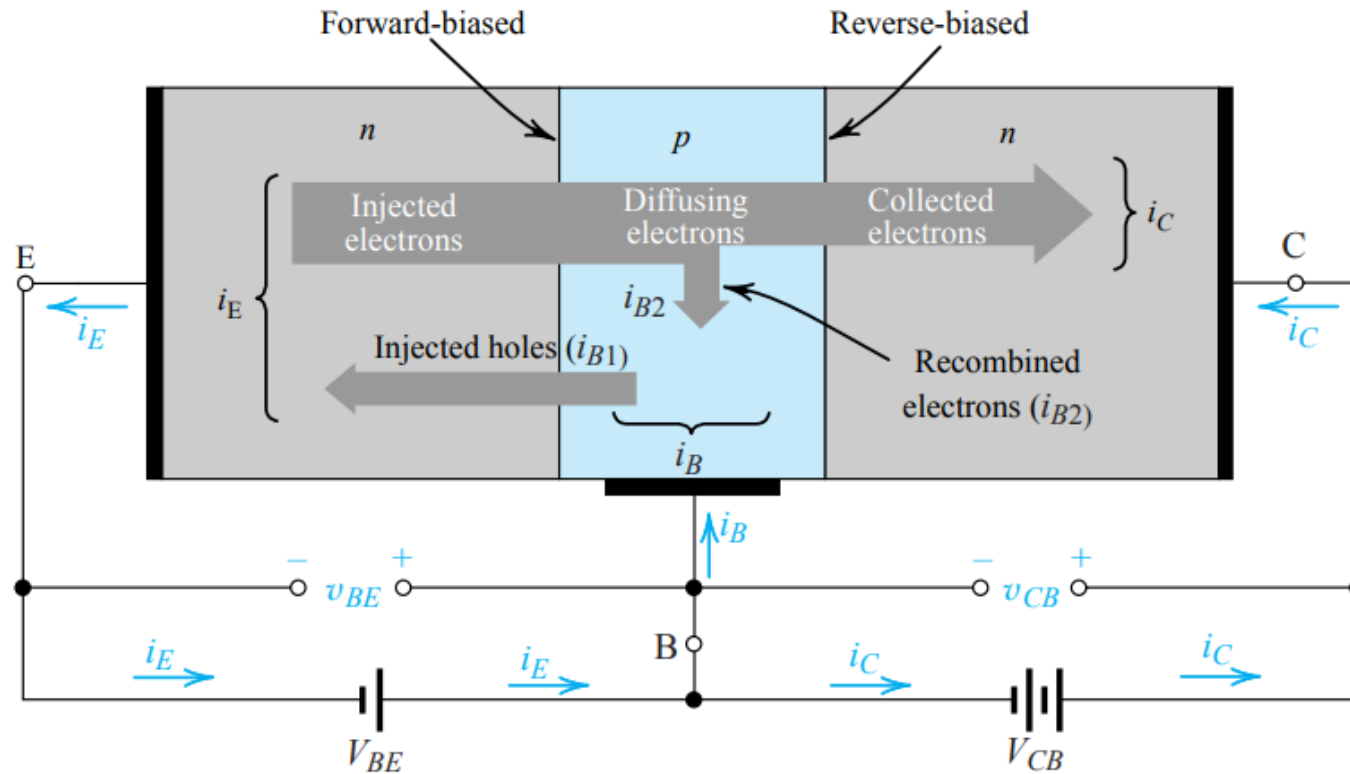
Unbiased Transistor

- A transistor has three doped regions: **Emitter, Base, Collector**
- **Doping Levels** - the **emitter is heavily doped**; the **base is lightly doped**; the **collector is intermediately doped**
- As a result of diffusion - **two depletion layers**
- the barrier potential is approx. 0.7 V at 25°C for silicon



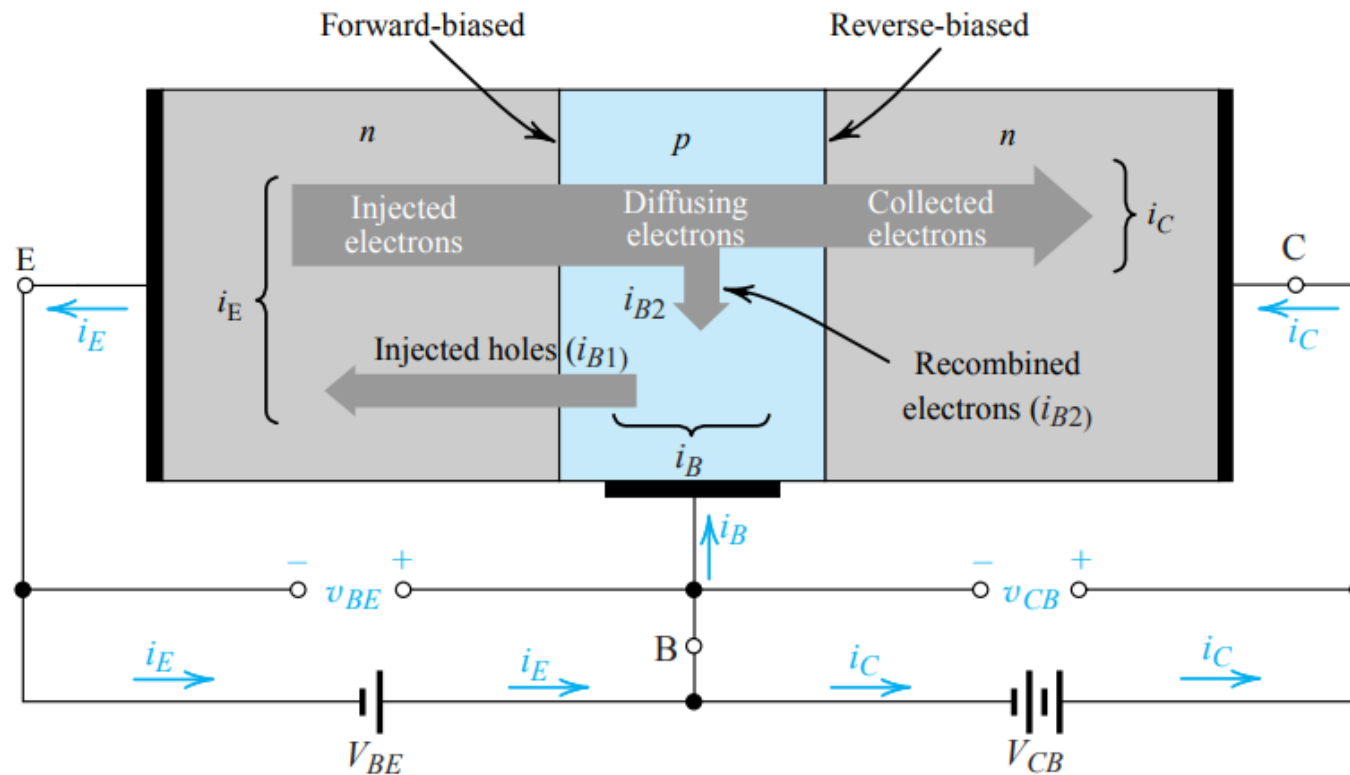
BJT Operation

- V_{BE} forward-biases the emitter diode
- V_{CB} reverse-biases the collector



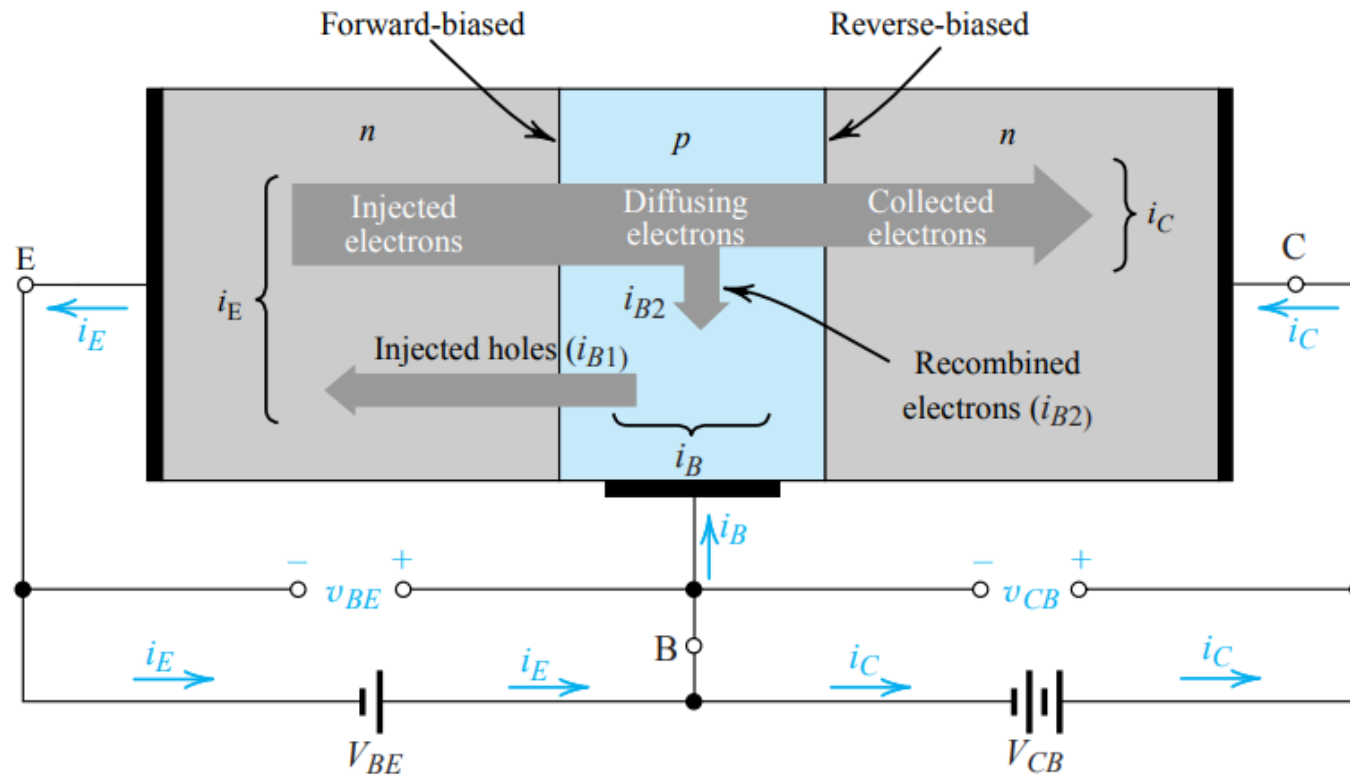
BJT Operation

- Heavily doped emitter emits or **injects its free electrons into the base**
- Holes diffuse from the base into the emitter
- Current through EB junction is **Emitter current, i_E**



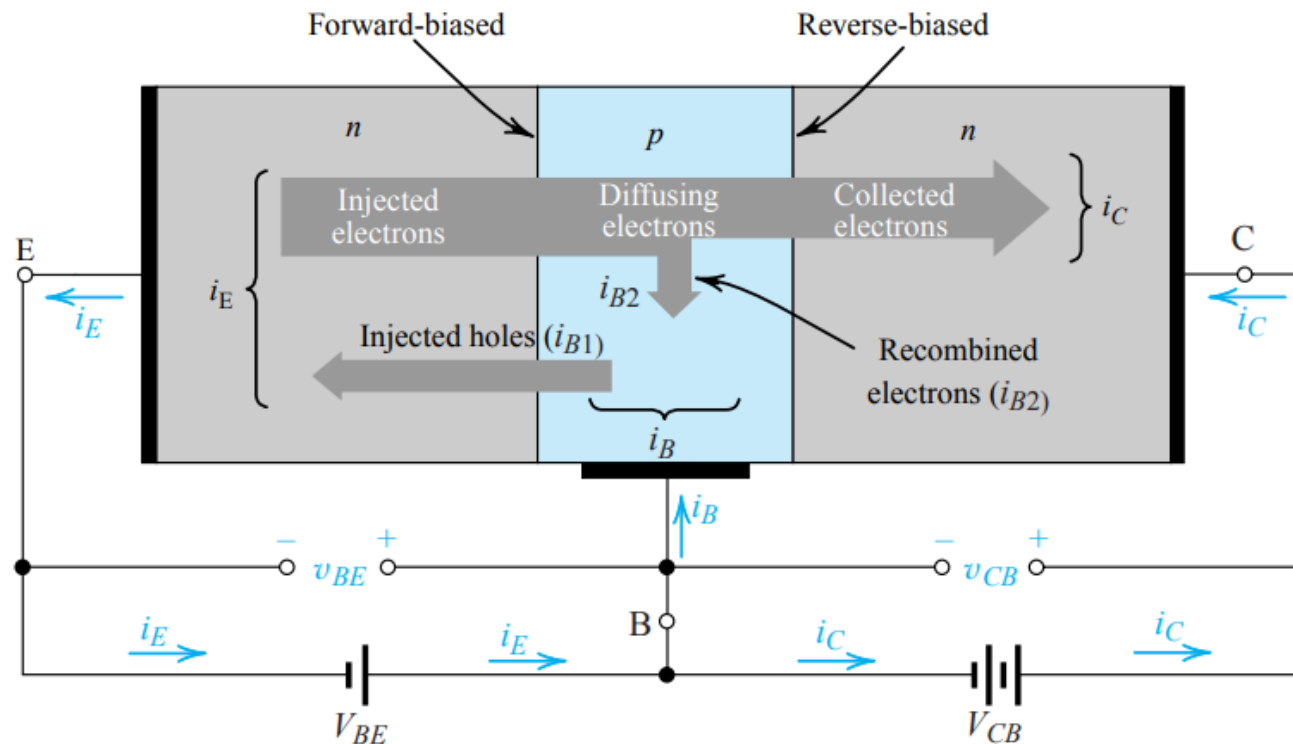
BJT Operation

- Lightly doped base passes emitter-injected electrons on to the collector.
- Only a few free electrons will **recombine** with holes in the lightly doped base
- Resulting in **Base current, i_B**



BJT Operation

- Most diffusing electrons will reach boundary of collector-base depletion region
- Because collector is more positive than base, these **electrons are swept into collector**
- Resulting in **Collector current, i_C**



Current Flow in BJT

- Three different currents in a transistor: emitter current i_E , base current i_B , and collector current i_C .

- Collector current, $i_C = I_S e^{v_{BE}/V_T}$

- Base current, i_B

$$i_B = \frac{i_C}{\beta}$$

$$i_B = \frac{I_S}{\beta} e^{v_{BE}/V_T}$$

β Common Emitter current gain

- Emitter current, $i_E = i_C + i_B$

$$i_E = \frac{\beta + 1}{\beta} i_C$$

$$\alpha = \frac{\beta}{\beta + 1}$$

$$\beta = \frac{\alpha}{1 - \alpha}$$

$$i_C = \alpha i_E$$

$$I_B \ll I_C$$

$$I_C \approx I_E$$

Transistor Currents

- **dc alpha** α_{dc} - dc collector current divided by the dc emitter current

$$\alpha_{dc} = \frac{I_C}{I_E}$$

- Collector current almost equals the emitter current, the dc alpha is slightly less than 1
- **dc beta** β_{dc} of a transistor - ratio of the dc collector current to the dc base current

$$\beta_{dc} = \frac{I_C}{I_B}$$

- dc beta is also known as the current gain because a small base current controls a much larger collector current.
- The current gain is typically 100 to 300

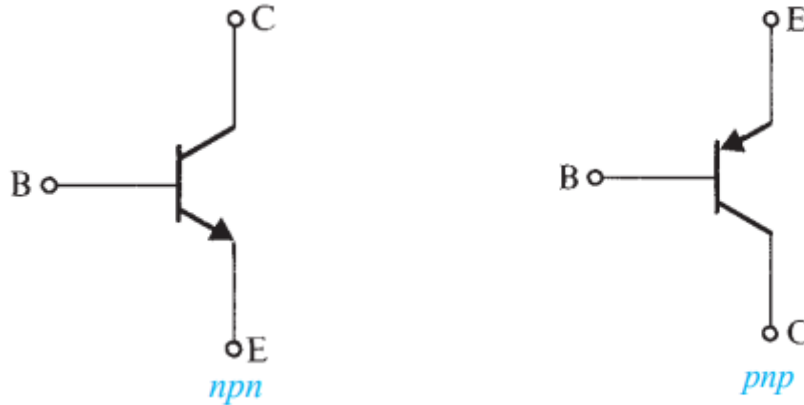
$$\alpha = \frac{\beta}{\beta + 1}, \quad \beta = \frac{\alpha}{1 - \alpha}$$

Modes of operation

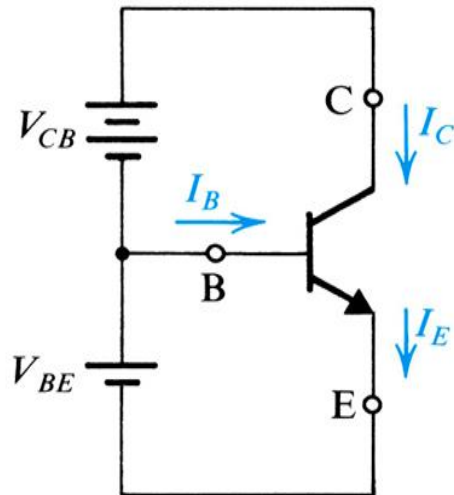
MODE	Emitter Base Junction (EBJ)	Collector Base Junction (CBJ)	Applications
Cut-off	Reverse Biased	Reverse Biased	Switch
Forward Active	Forward Biased	Reverse Biased	Amplifier
Reverse Active	Reverse Biased	Forward Biased	Mostly not operated in this mode
Saturation	Forward Biased	Forward Biased	Switch

Circuit Symbols and Conventions

- BJT circuit symbol



- *npn* transistor biased in active mode



npn transistor will operate in active mode as long as the collector voltage does not fall below that of the base by approximately 0.4 V

$V_{CB} < 0.4$ V transistor leaves active mode and enters saturation mode

Circuit Symbols and Conventions

The Collector-Base Reverse Current (I_{CB0})

- Previously, small **reverse current was ignored**.
 - This is carried by **thermally-generated minority** carriers.
- The **collector-base junction current** (I_{CB0}) is the reverse current flowing from collector to base with the emitter open-circuited.
 - Usually in **nanoampere range**
- I_{CB0} depends on temperature, approx. **doubling for every 10⁰C rise**

Summary of BJT current-voltage relationship

$$i_C = I_S e^{v_{BE}/V_T}$$

$$i_B = \frac{i_C}{\beta} = \left(\frac{I_S}{\beta}\right) e^{v_{BE}/V_T}$$

$$i_E = \frac{i_C}{\alpha} = \left(\frac{I_S}{\alpha}\right) e^{v_{BE}/V_T}$$

Note: For the *pnp* transistor, replace v_{BE} with v_{EB} .

$$i_C = \alpha i_E \qquad i_B = (1 - \alpha) i_E = \frac{i_E}{\beta + 1}$$

$$i_C = \beta i_B \qquad i_E = (\beta + 1) i_B$$

$$\beta = \frac{\alpha}{1 - \alpha} \qquad \alpha = \frac{\beta}{\beta + 1}$$

$$V_T = \text{thermal voltage} = \frac{kT}{q} \simeq 25 \text{ mV at room temperature}$$

Problem #1

A transistor has a collector current of 10 mA and a base current of 40 μ A. What is the current gain of the transistor?

Solution

$$\beta_{dc} = \frac{10 \text{ mA}}{40 \mu\text{A}} = 250$$

Problem #2

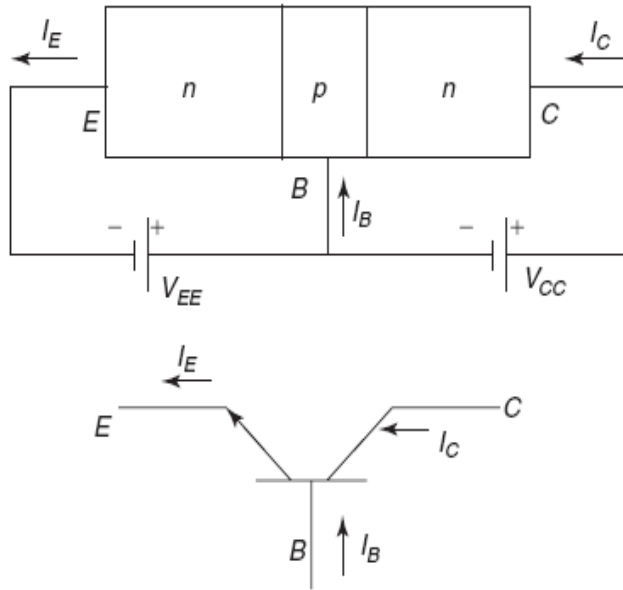
A transistor has a current gain of 175. If the base current is 0.1 mA, what is the collector current?

Solution

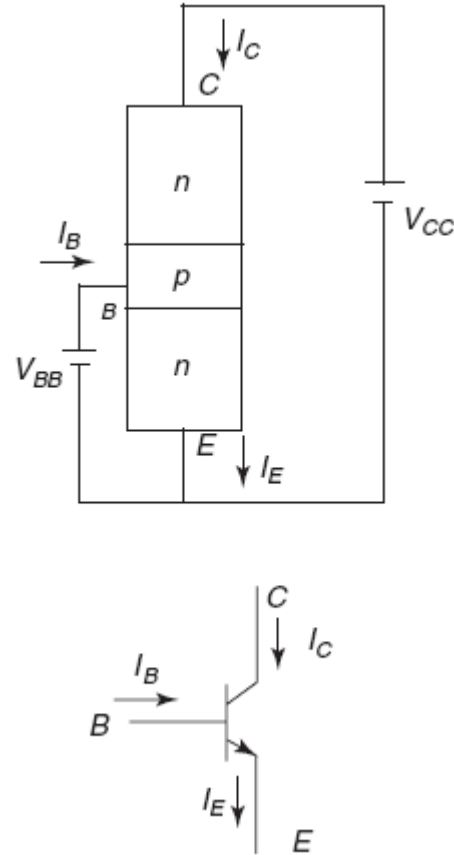
$$I_C = 175(0.1 \text{ mA}) = 17.5 \text{ mA}$$

BJT Configurations

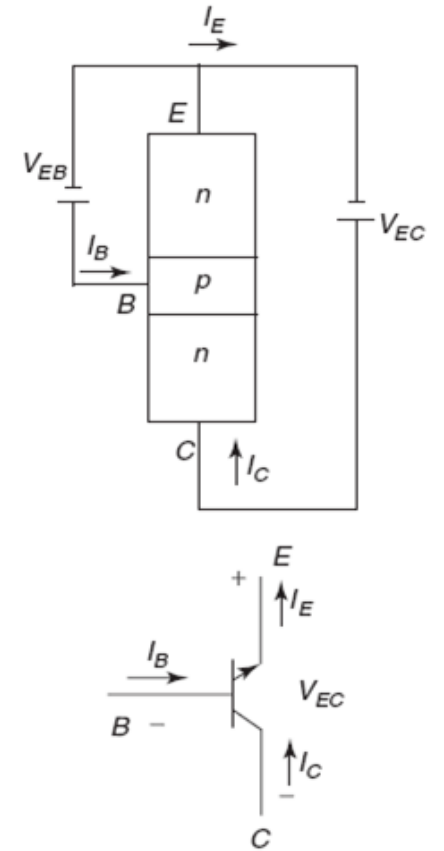
**Common-base configuration
of npn transistor**



**Common-emitter configuration
of npn transistor**



**Common-collector configuration
of npn transistor**



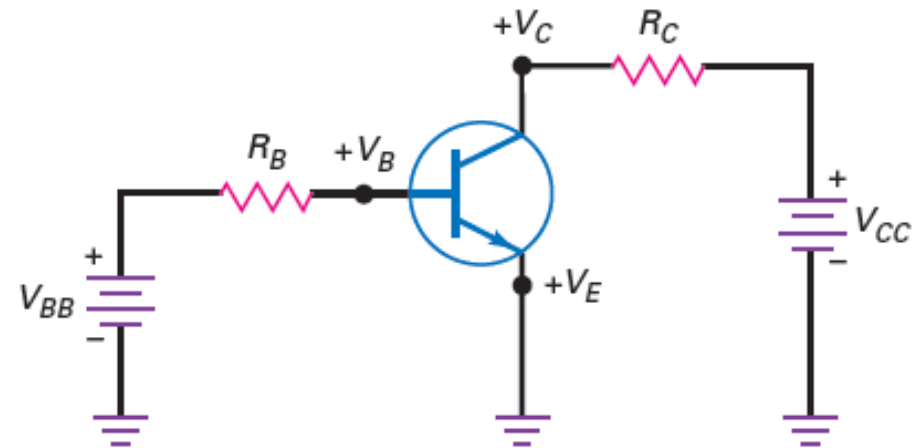
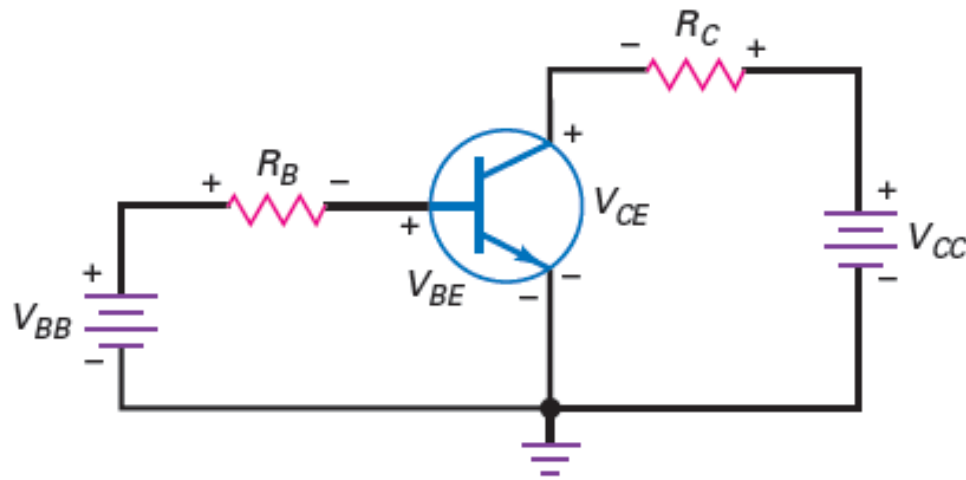
Transistor Characteristics

Common Emitter Characteristics

Transistor Characteristics

Common Emitter Configuration

- V_{BB} source forward-biases the emitter diode with R_B as a current-limiting resistance.
- By changing V_{BB} or R_B , the base current can be changed.
- Changing the base current will change the collector current.
- The **base current controls the collector current.**



Transistor Characteristics

Common Emitter Configuration

- Source voltage V_{CC} reverse-biases the collector diode through R_C .
- The collector must be positive to collect most of the free electrons injected into the base.

$$V_{CE} = V_C - V_E$$

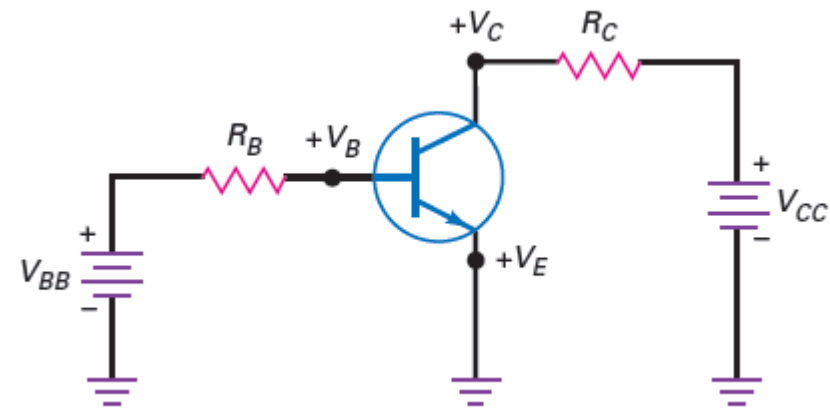
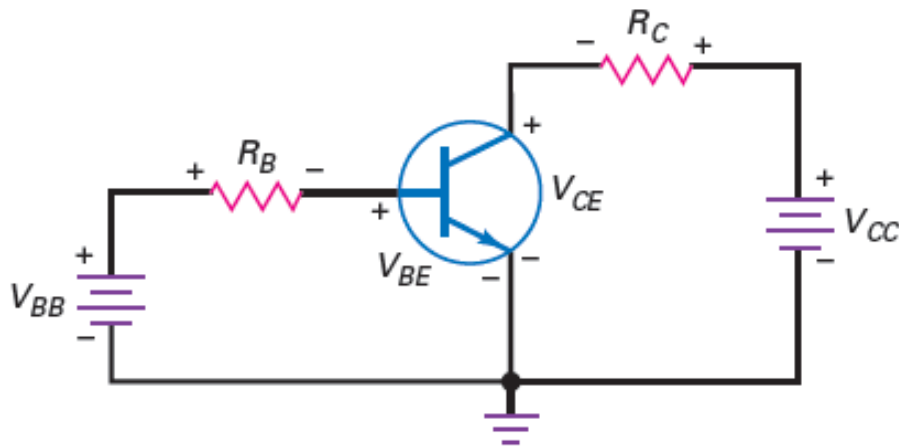
$$V_{CB} = V_C - V_B \quad V_E \text{ is zero in CE connection}$$

$$V_{BE} = V_B - V_E$$

$$V_{CE} = V_C$$

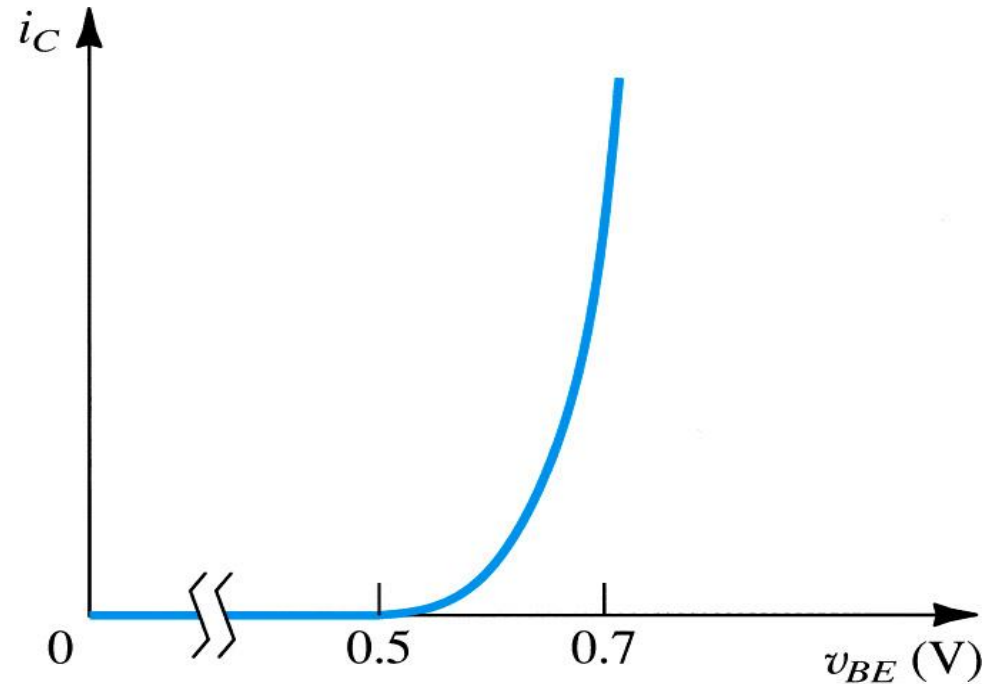
$$V_{CB} = V_C - V_B$$

$$V_{BE} = V_B$$



Graphical Representation of transistor $i-v$ Characteristics

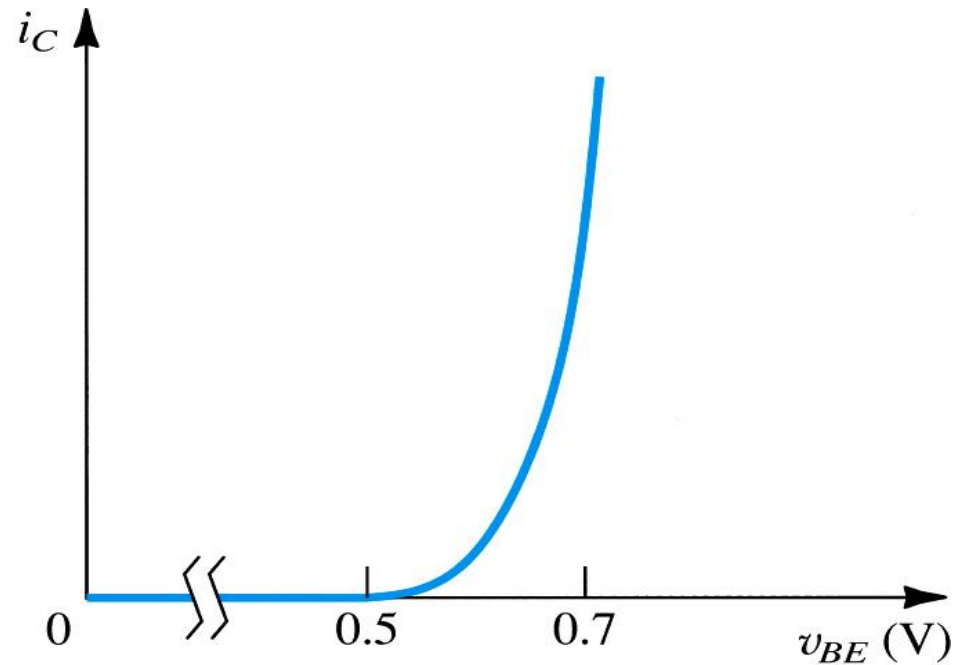
Common Emitter Characteristics



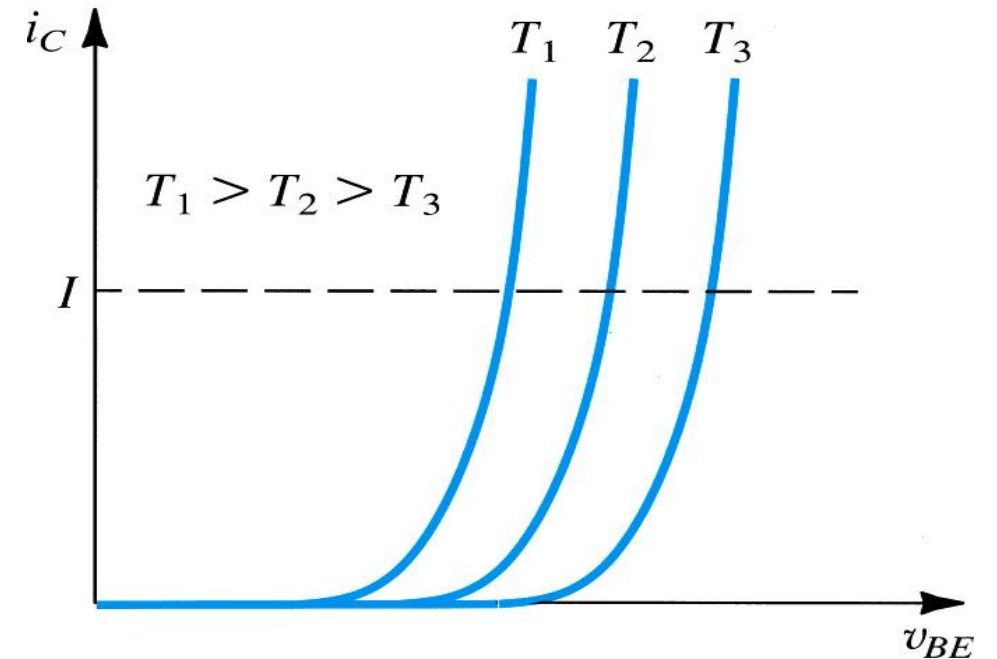
The i_C-v_{BE} characteristic for an npn transistor.

Graphical Representation of transistor $i-v$ Characteristics

Common Emitter Characteristics



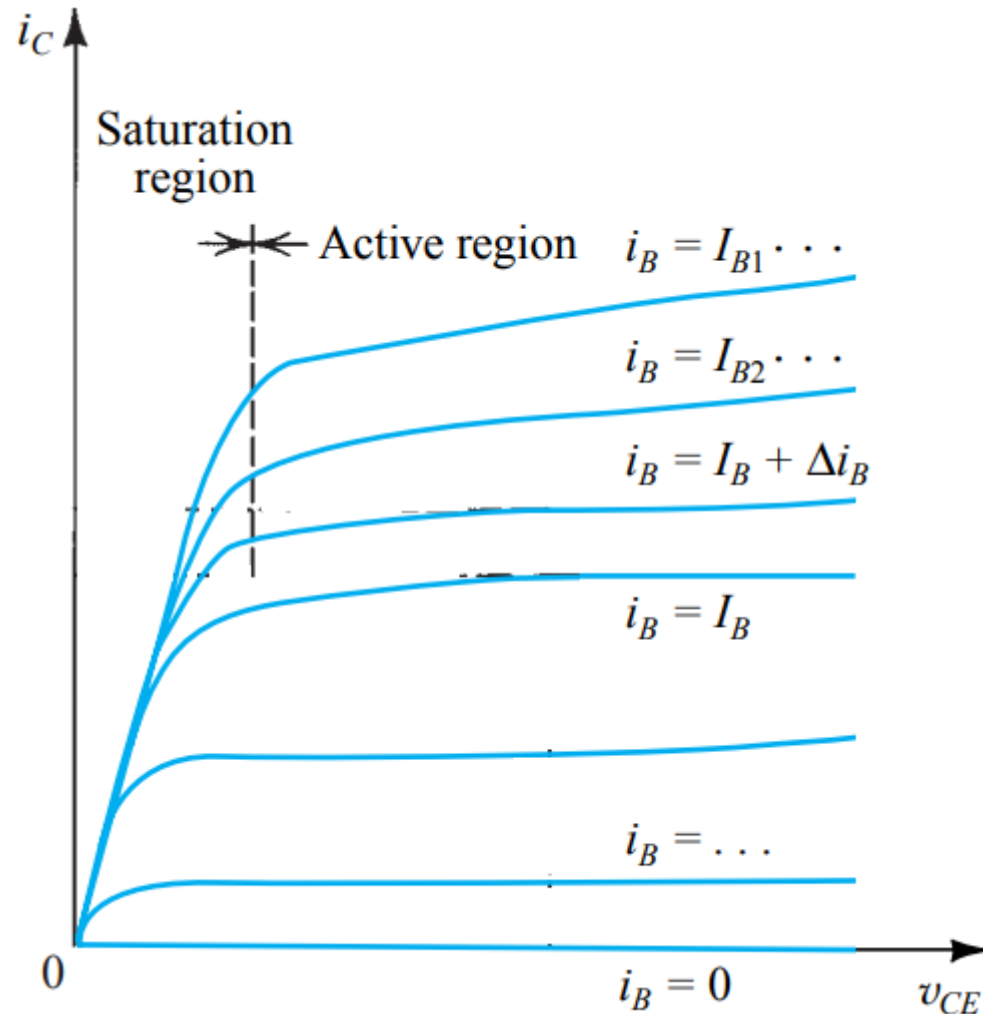
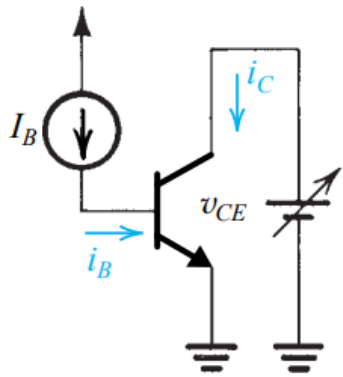
The i_C-v_{BE} characteristic for an npn transistor



Effect of temperature on the i_C-v_{BE} characteristic

Graphical Representation of transistor $i-v$ Characteristics

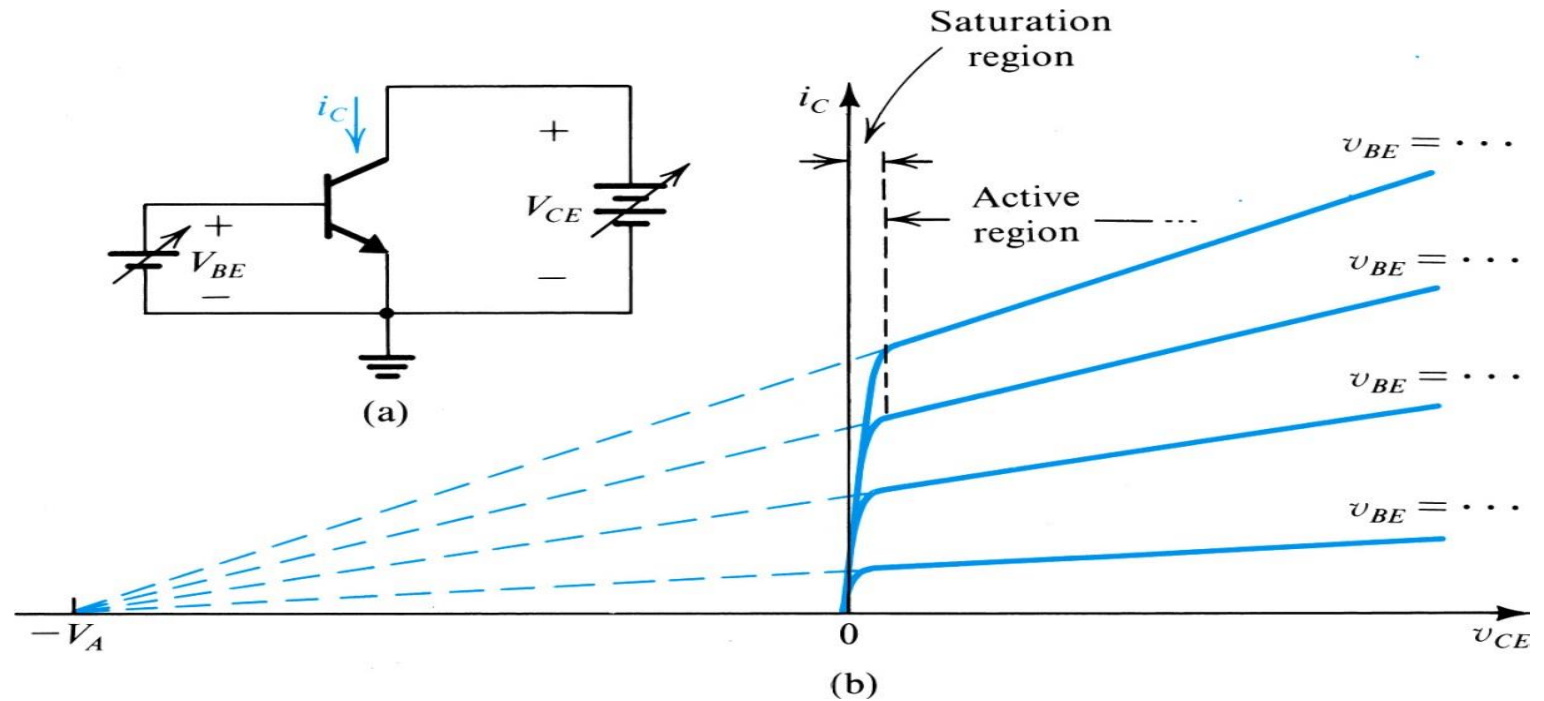
Common Emitter Characteristics



The i_C-v_{CE} characteristic for an npn transistor.

Dependence of i_C on Collector Voltage – The Early Effect

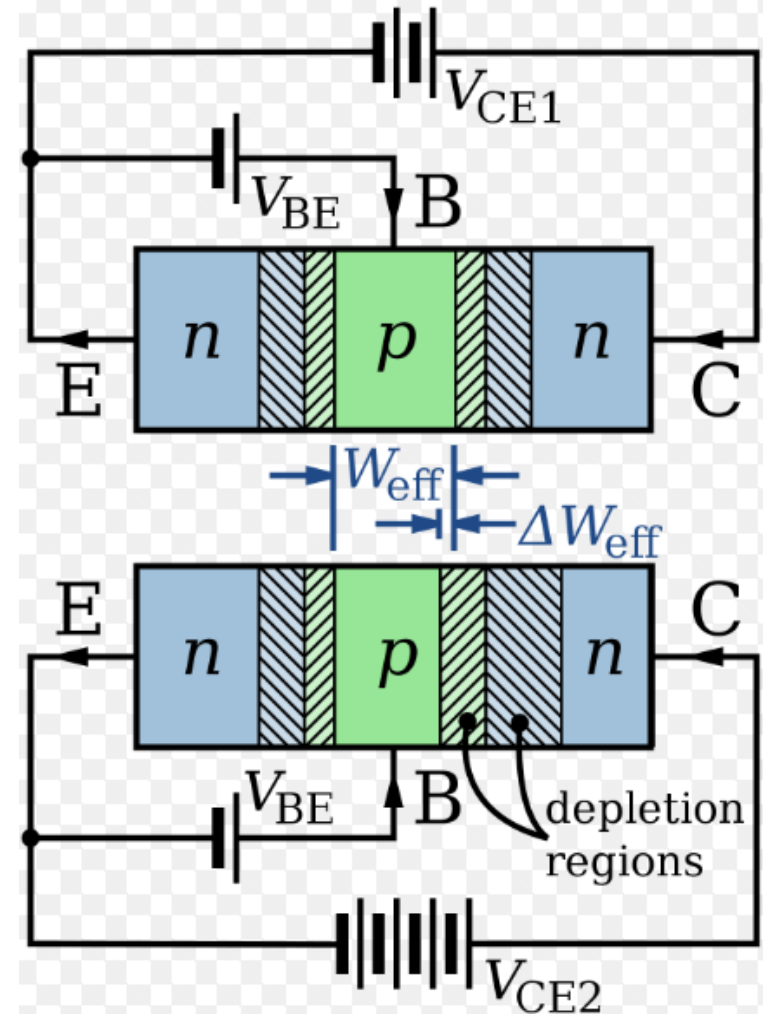
- When operated in active region, practical BJT's show some **dependence of collector current on collector voltage**.
- As such, i_C - v_{CE} characteristic is **not “straight”**.



V_A - Early Voltage (50 – 100 V)

Early Effect

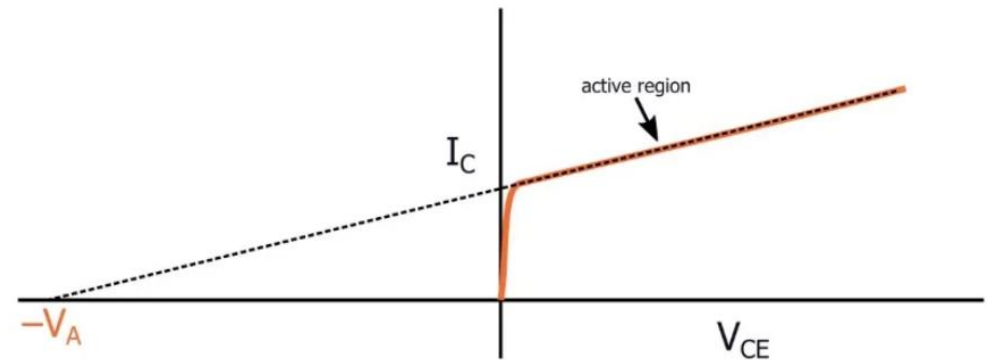
- Early effect or base width modulation: is the **variation in the width of the base** due to a variation in the **applied base-to-collector voltage**.
- For example a **greater** reverse bias across the collector- base junction **increases the collector-base depletion width**.



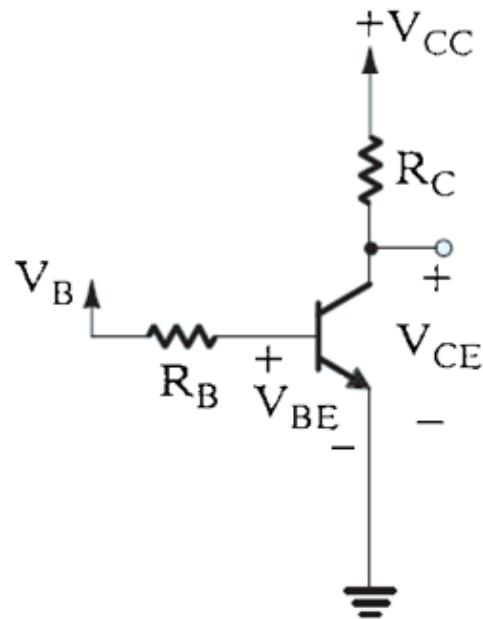
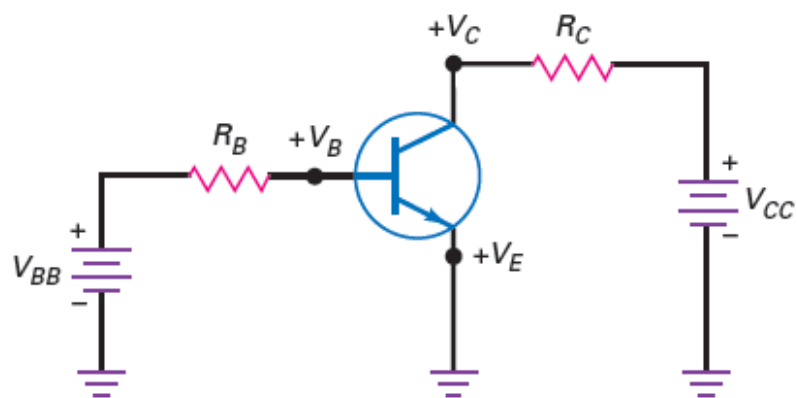
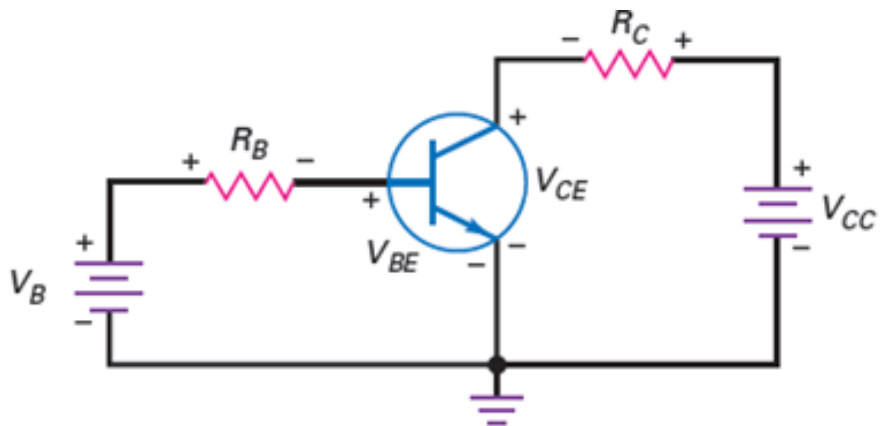
Consequences of Early Effect

- Reverse saturation current increases, increasing the collector current. $I_C = I_S e^{\frac{V_{BE}}{V_T}}$
- Less chance for recombination in the base.
- Charge gradient is increased and hence the minority carriers injected inside the emitter will increase.
- For extremely **large voltages**, base width = 0 , causing voltage breakdown in transistor resulting in **punchthrough**.

$$I_C = I_S e^{\frac{V_{BE}}{V_T}} \left(1 + \frac{V_{CE}}{V_A} \right)$$



Transistor Operating Point



Applying KVL

$$V_B = I_B R_B + V_{BE}$$

$$I_B = \frac{V_B - V_{BE}}{R_B}$$

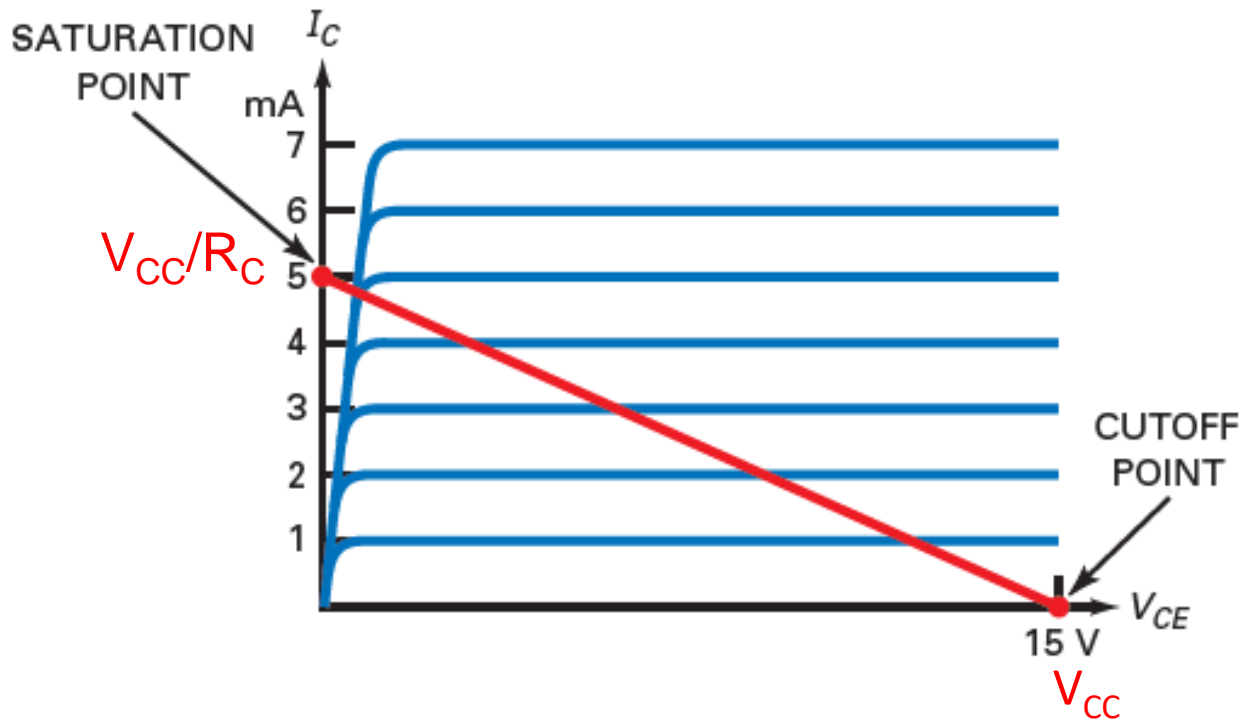
$$V_{CC} = I_C R_C + V_{CE}$$

$$I_C = \frac{V_{CC}}{R_C} - \frac{V_{CE}}{R_C}$$

$$P_D = V_{CE} I_C$$

DC Load Line

- In graphical analysis of nonlinear electronic circuits, a **load line** is a **line** drawn on the characteristic curve, a graph of the current vs the voltage
- It is used to determine the correct **DC operating point**, often called the **Q point**.



$$V_{CC} = I_C R_C + V_{CE}$$

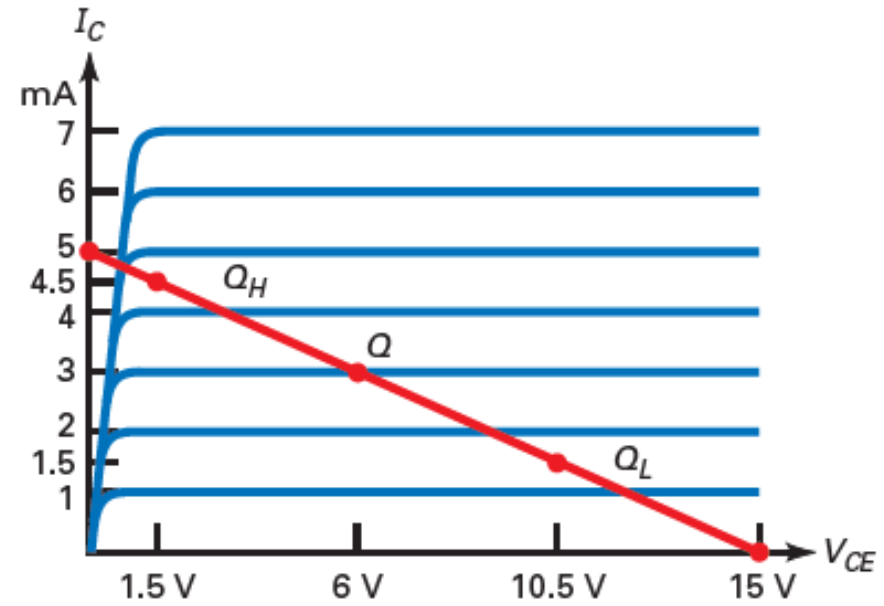
$$I_C = \frac{V_{CC}}{R_C} - \frac{V_{CE}}{R_C}$$

Operating Point (Q-Point)

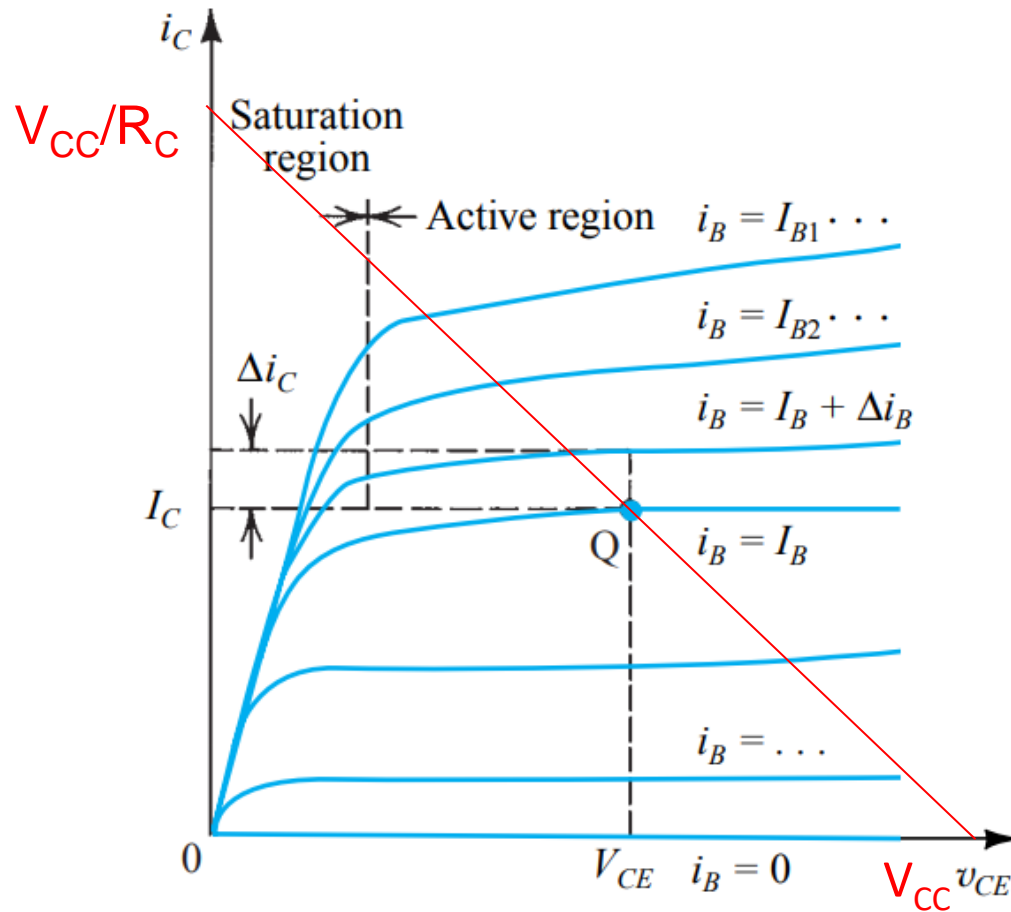
$$I_B = \frac{V_{BB} - V_{BE}}{R_B}$$

$$I_C = \beta_{dc} I_B$$

$$V_{CE} = V_{CC} - I_C R_C$$



Operating Point (Q-Point)

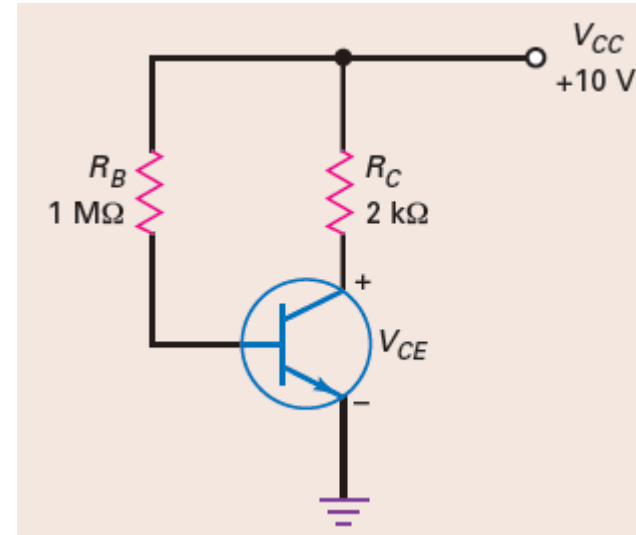


$$V_{CC} = I_C R_C + V_{CE}$$

$$I_C = \frac{V_{CC}}{R_C} - \frac{V_{CE}}{R_C}$$

Problem #3

The transistor shown below has $\beta_{dc} = 300$. Calculate I_B , I_C , V_{CE} , and P_D .



Solution

$$I_B = 9.3\ \mu\text{A}$$

$$I_C = 2.79\ \text{mA}$$

$$V_{CE} = 4.42\ \text{V}$$

$$P_D = 12.3\ \text{mW}$$

2N3904 / MMBT3904 / PZT3904 NPN General Purpose Amplifier

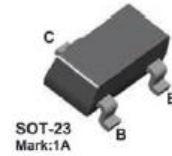
Features

- This device is designed as a general purpose amplifier and switch.
- The useful dynamic range extends to 100 mA as a switch and to 100 MHz as an amplifier.

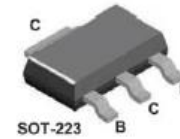
2N3904



MMBT3904



PZT3904



Absolute Maximum Ratings* $T_a = 25^\circ\text{C}$ unless otherwise noted

Symbol	Parameter	Value	Units
V_{CE0}	Collector-Emitter Voltage	40	V
V_{CBO}	Collector-Base Voltage	60	V
V_{EBO}	Emitter-Base Voltage	6.0	V
I_C	Collector Current - Continuous	200	mA
T_J, T_{stg}	Operating and Storage Junction Temperature Range	-55 to +150	$^\circ\text{C}$

* These ratings are limiting values above which the serviceability of any semiconductor device may be impaired.

NOTES:

- 1) These ratings are based on a maximum junction temperature of 150 degrees C.
- 2) These are steady state limits. The factory should be consulted on applications involving pulsed or low duty cycle operations.

Thermal Characteristics $T_a = 25^\circ\text{C}$ unless otherwise noted

Symbol	Parameter	Max.			Units
		2N3904	*MMBT3904	**PZT3904	
P_D	Total Device Dissipation Derate above 25°C	625	350	1,000	mW
		5.0	2.8	8.0	$\text{mW}/^\circ\text{C}$
$R_{\theta JC}$	Thermal Resistance, Junction to Case	83.3			$^\circ\text{C}/\text{W}$
$R_{\theta JA}$	Thermal Resistance, Junction to Ambient	200	357	125	$^\circ\text{C}/\text{W}$

* Device mounted on FR-4 PCB 1.6" X 1.6" X 0.06".

** Device mounted on FR-4 PCB 36 mm X 18 mm X 1.5 mm; mounting pad for the collector lead min. 6 cm^2 .

Electrical Characteristics $T_a = 25^\circ\text{C}$ unless otherwise noted

Symbol	Parameter	Test Condition	Min.	Max.	Units
OFF CHARACTERISTICS					
$V_{(BR)CEO}$	Collector-Emitter Breakdown Voltage	$I_C = 1.0\text{mA}, I_B = 0$	40		V
$V_{(BR)CBO}$	Collector-Base Breakdown Voltage	$I_C = 10\mu\text{A}, I_E = 0$	60		V
$V_{(BR)EBO}$	Emitter-Base Breakdown Voltage	$I_E = 10\mu\text{A}, I_C = 0$	6.0		V
I_{BL}	Base Cutoff Current	$V_{CE} = 30\text{V}, V_{EB} = 3\text{V}$		50	nA
I_{CEX}	Collector Cutoff Current	$V_{CE} = 30\text{V}, V_{EB} = 3\text{V}$		50	nA
ON CHARACTERISTICS*					
h_{FE}	DC Current Gain	$I_C = 0.1\text{mA}, V_{CE} = 1.0\text{V}$ $I_C = 1.0\text{mA}, V_{CE} = 1.0\text{V}$ $I_C = 10\text{mA}, V_{CE} = 1.0\text{V}$ $I_C = 50\text{mA}, V_{CE} = 1.0\text{V}$ $I_C = 100\text{mA}, V_{CE} = 1.0\text{V}$	40 70 100 60 30	300	
$V_{CE(sat)}$	Collector-Emitter Saturation Voltage	$I_C = 10\text{mA}, I_B = 1.0\text{mA}$ $I_C = 50\text{mA}, I_B = 5.0\text{mA}$		0.2 0.3	V V
$V_{BE(sat)}$	Base-Emitter Saturation Voltage	$I_C = 10\text{mA}, I_B = 1.0\text{mA}$ $I_C = 50\text{mA}, I_B = 5.0\text{mA}$	0.65	0.85 0.95	V V
SMALL SIGNAL CHARACTERISTICS					
f_T	Current Gain - Bandwidth Product	$I_C = 10\text{mA}, V_{CE} = 20\text{V},$ $f = 100\text{MHz}$	300		MHz
C_{obo}	Output Capacitance	$V_{CB} = 5.0\text{V}, I_E = 0,$ $f = 1.0\text{MHz}$		4.0	pF
C_{ibo}	Input Capacitance	$V_{EB} = 0.5\text{V}, I_C = 0,$ $f = 1.0\text{MHz}$		8.0	pF
NF	Noise Figure	$I_C = 100\mu\text{A}, V_{CE} = 5.0\text{V},$ $R_S = 1.0\text{k}\Omega,$ $f = 10\text{Hz to } 15.7\text{kHz}$		5.0	dB
SWITCHING CHARACTERISTICS					
t_d	Delay Time	$V_{CC} = 3.0\text{V}, V_{BE} = 0.5\text{V}$		35	ns
t_r	Rise Time	$I_C = 10\text{mA}, I_{B1} = 1.0\text{mA}$		35	ns
t_s	Storage Time	$V_{CC} = 3.0\text{V}, I_C = 10\text{mA},$ $I_{B1} = I_{B2} = 1.0\text{mA}$		200	ns
t_f	Fall Time			50	ns

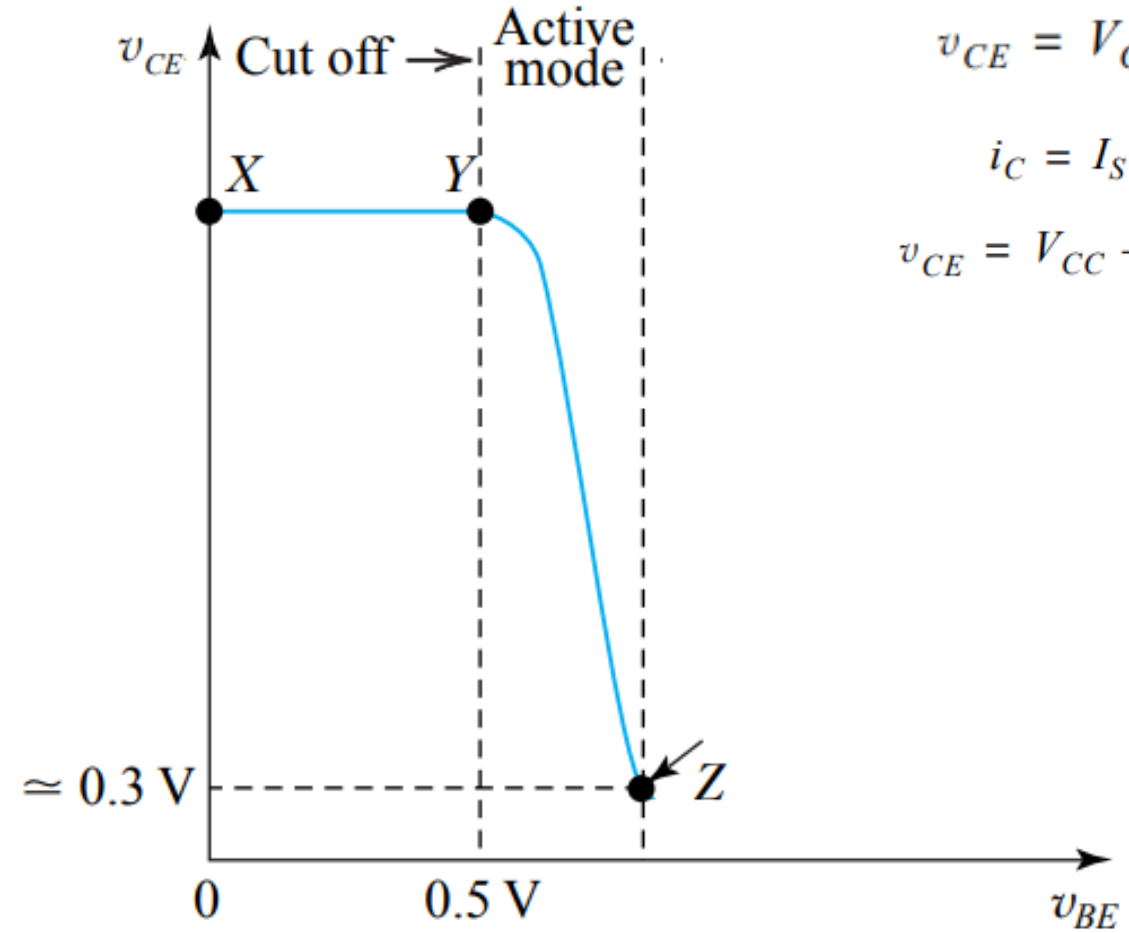
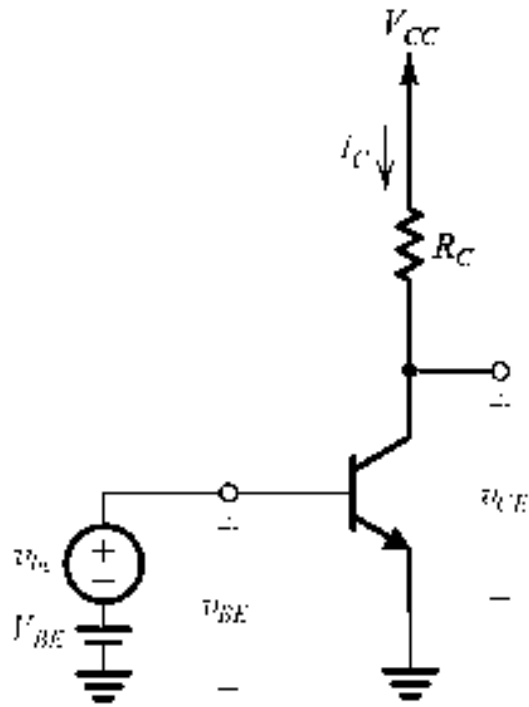
* Pulse Test: Pulse Width $\leq 300\mu\text{s}$, Duty Cycle $\leq 2.0\%$

ON CHARACTERISTICS*					
h_{FE}	DC Current Gain	$I_C = 0.1\text{mA}, V_{CE} = 1.0\text{V}$	40		
		$I_C = 1.0\text{mA}, V_{CE} = 1.0\text{V}$	70		
		$I_C = 10\text{mA}, V_{CE} = 1.0\text{V}$	100	300	
		$I_C = 50\text{mA}, V_{CE} = 1.0\text{V}$	60		
		$I_C = 100\text{mA}, V_{CE} = 1.0\text{V}$	30		
$V_{CE(\text{sat})}$	Collector-Emitter Saturation Voltage	$I_C = 10\text{mA}, I_B = 1.0\text{mA}$		0.2	V
		$I_C = 50\text{mA}, I_B = 5.0\text{mA}$		0.3	V
$V_{BE(\text{sat})}$	Base-Emitter Saturation Voltage	$I_C = 10\text{mA}, I_B = 1.0\text{mA}$	0.65	0.85	V
		$I_C = 50\text{mA}, I_B = 5.0\text{mA}$		0.95	V

BJT as an Amplifier

Common Emitter Amplifier

Voltage amplifier



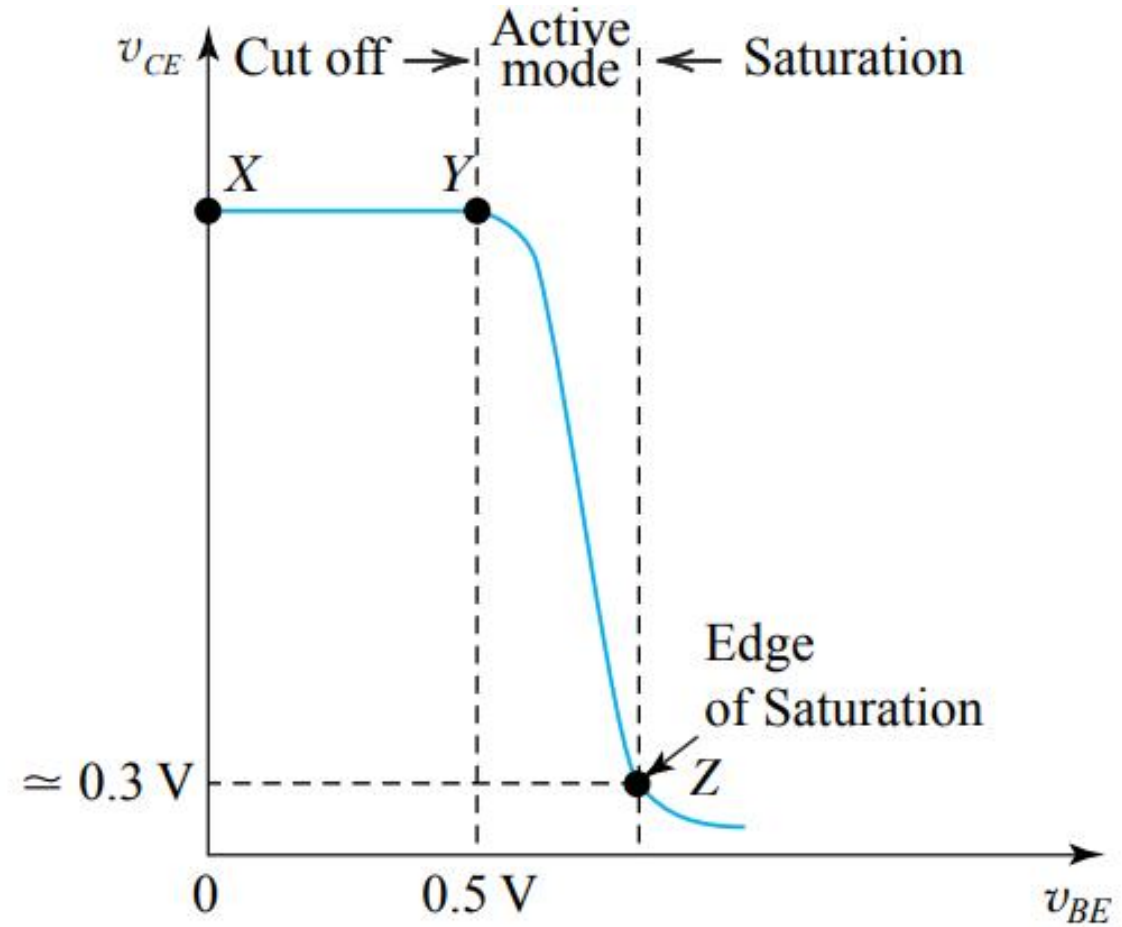
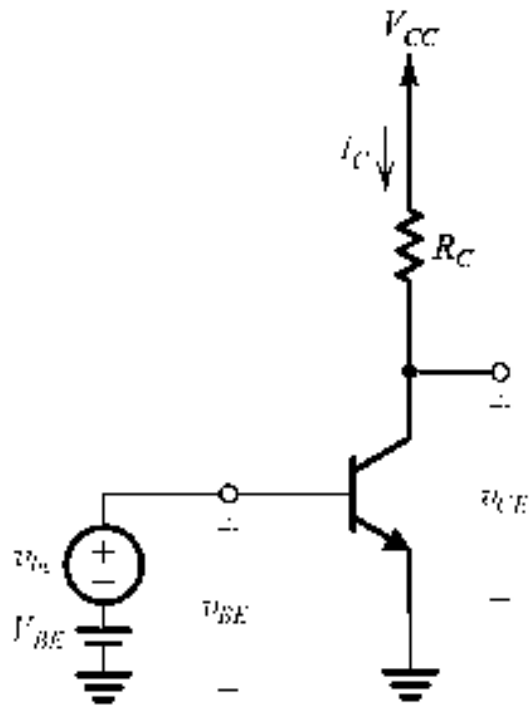
$$v_{CE} = V_{CC} - i_C R_C$$

$$i_C = I_S e^{v_{BE}/V_T}$$

$$v_{CE} = V_{CC} - R_C I_S e^{v_{BE}/V_T}$$

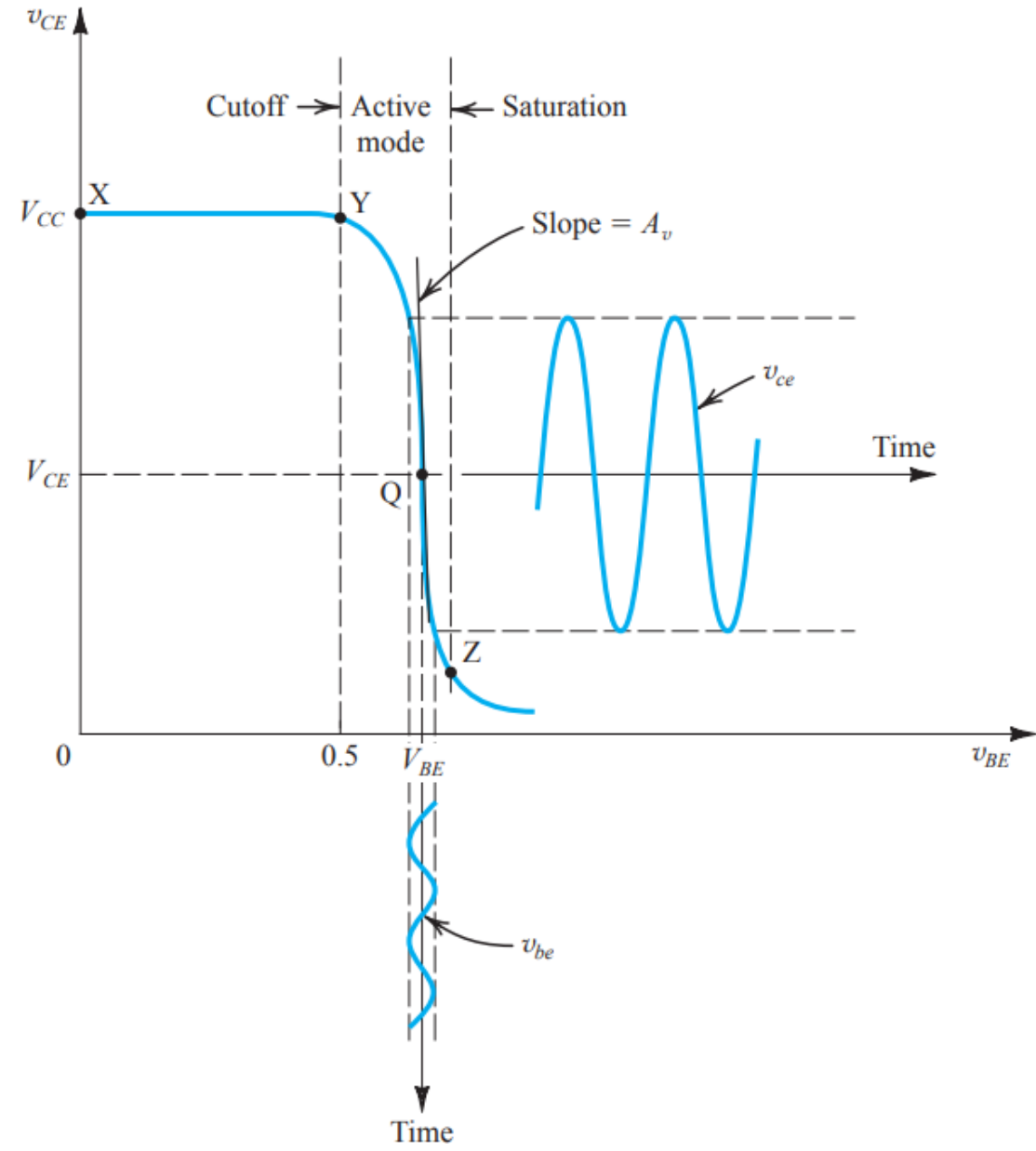
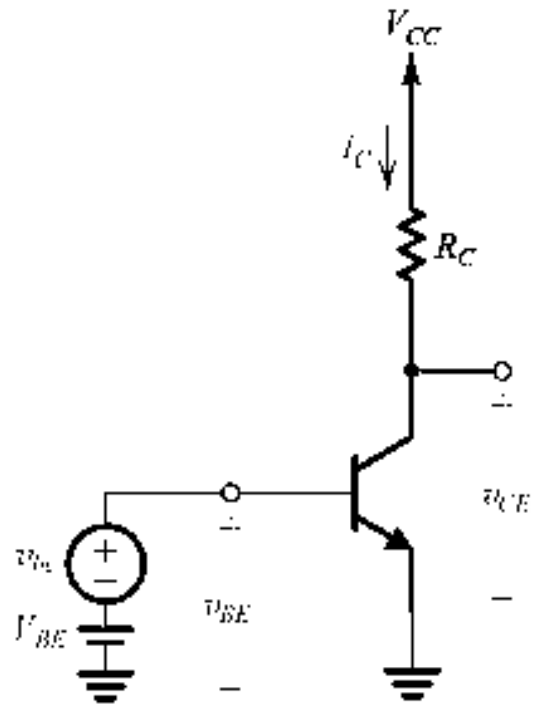
Common Emitter Amplifier

Voltage amplifier



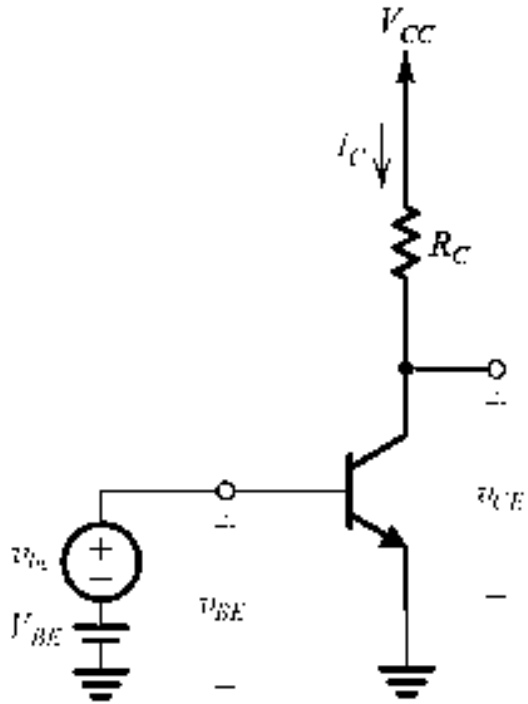
Common Emitter Amplifier

Voltage amplifier



Common Emitter Amplifier

Voltage amplifier



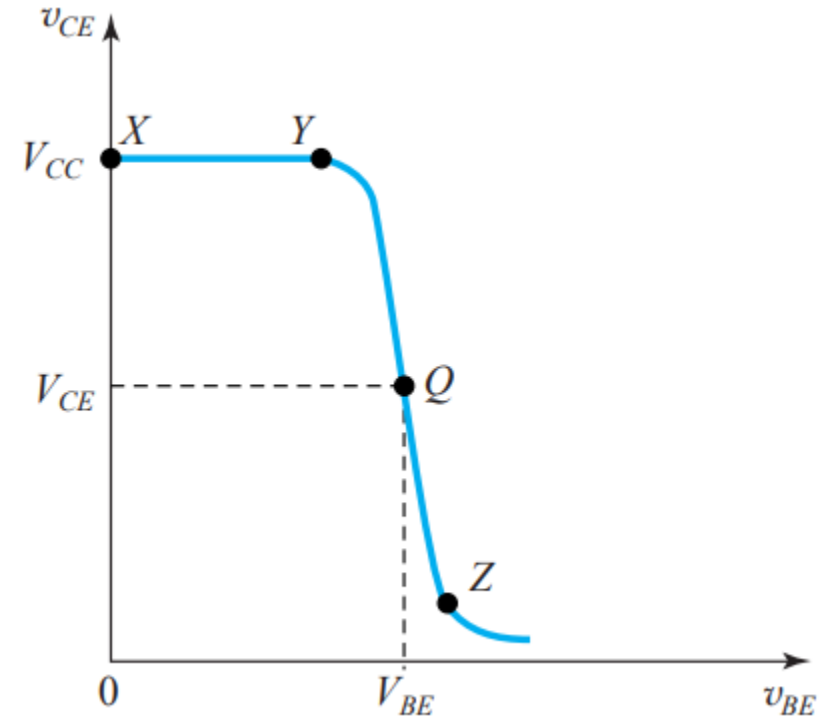
Voltage gain $A_v \equiv \left. \frac{dv_{CE}}{dv_{BE}} \right|_{v_{BE} = V_{BE}}$

$$v_{CE} = V_{CC} - i_C R_C$$

$$v_{CE} = V_{CC} - R_C I_S e^{v_{BE}/V_T}$$

$$A_v = -\left(\frac{I_C}{V_T}\right) R_C$$

$$A_v = -\frac{I_C R_C}{V_T}$$

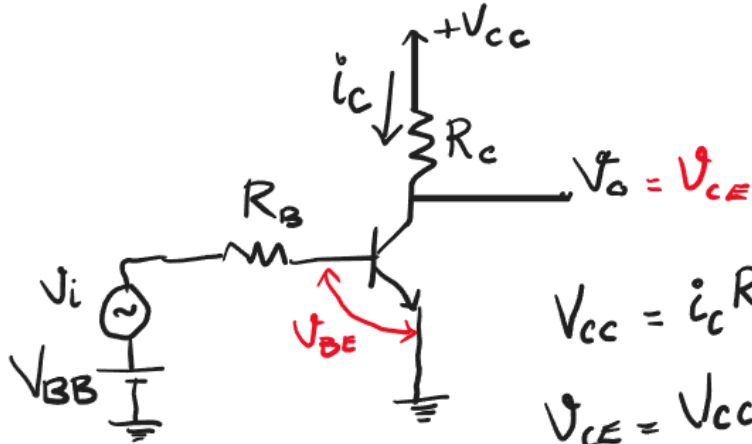


Common Emitter Amplifier

Voltage amplifier

BJT as Amplifier

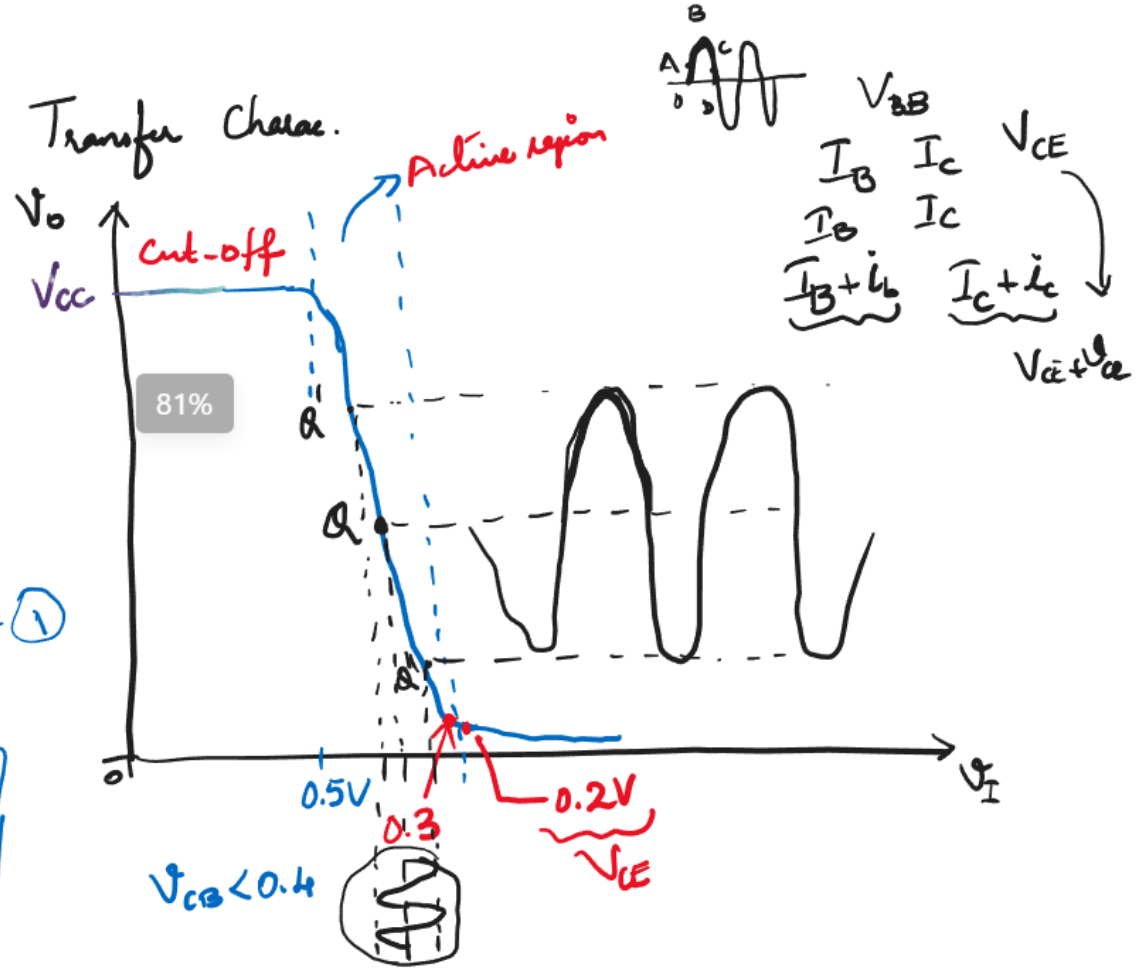
i_c i_b i_e } Bias + Signal
 I_C I_B I_E } i_c i_b i_e



$$V_{CC} = i_c R_C + V_{CE} \quad \text{--- (1)}$$

$$V_{CE} = V_{CC} - i_c R_C$$

10	-	1	=	9V
10	-	4	=	6
10	-	6	=	4
10	-	10	=	0



Common Emitter Amplifier

Voltage amplifier

$$V_o = V_{CE} = V_{CC} - i_c R_c \quad \text{①}$$

$$i_c = I_s e^{v_{BE}/V_T}$$

$$V_o = V_{CC} - R_c I_s e^{v_{BE}/V_T}$$

Voltage gain, $A_v = \frac{\Delta V_o}{\Delta V_i}$

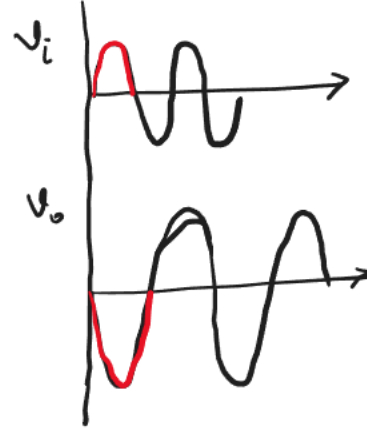
$$A_v = \left. \frac{dV_o}{dV_i} \right|_{v_i = v_{BE}}$$

$$A_v = 0 - \frac{1}{V_T} \cdot I_s e^{v_{BE}/V_T} \cdot R_c$$

$$= - \frac{R_c \cdot I_s e^{v_{BE}/V_T}}{V_T} = - \frac{R_c \cdot i_c}{V_T}$$

$$= - \frac{i_c R_c}{V_T}$$

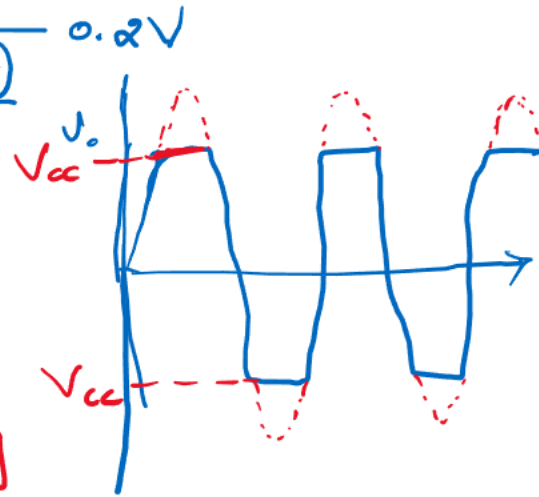
$$A_v = - \frac{i_c R_c}{V_T}$$



180° phase shift
CE →

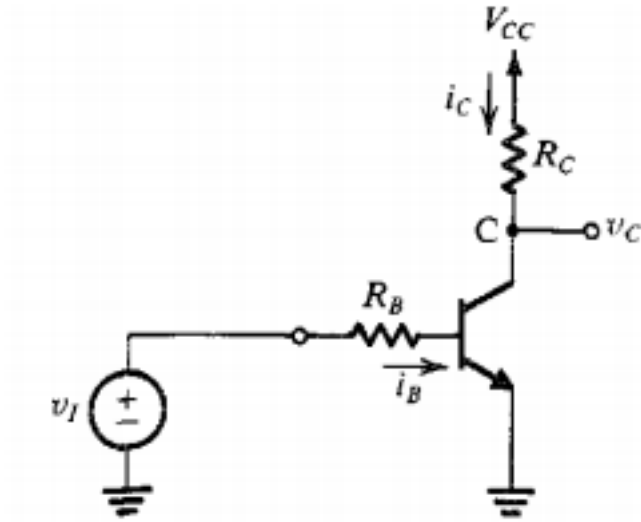
$$A_v = - \frac{(V_{CC} - V_{CE})}{V_T} \quad 0.2V$$

$$A_v \approx - \frac{V_{CC}}{V_T}$$



Signal Swing

Operation as Switch



$$i_B = \frac{v_I - V_{BE}}{R_B}$$

$$i_C = \beta i_B$$

$$v_C = V_{CC} - R_C i_C$$

$$I_{C(\text{EOS})} = \frac{V_{CC} - 0.3}{R_C}$$

$$I_{C\text{sat}} = \frac{V_{CC} - V_{CE\text{sat}}}{R_C}$$

$$\beta_{\text{forced}} \equiv \frac{I_{C\text{sat}}}{I_B}$$

$$\beta_{\text{forced}} < \beta_F$$

Operation as Switch

BJT as a Switch

$$V_I = i_B R_B + V_{BE}$$

$$i_B = \frac{V_I - V_{BE}}{R_B}$$

$$i_C = \beta i_B$$

$$V_{CE} = V_{CC} - i_C R_C$$

EOS - Edge of Saturation

$$\begin{aligned} I_{C(EOS)} &= \frac{V_{CC} - V_{CE} = 0.3V}{R_C} \\ &= \frac{V_{CC} - 0.3}{R_C} \end{aligned}$$

$$I_{B(EOS)} = \frac{I_{C(EOS)}}{\beta}$$

$$I_{C(sat)} = \frac{V_{CC} - V_{CE(sat)} = 0.2V}{R_C}$$

(i) $V_{CE} = V_{CC}$ Cutoff

(ii) $V_{CE} = V_{CC}/2$ Active

(iii) $V_{CE} = 0.2V$ Saturation

$$\beta_{forced} = \frac{I_{C(sat)}}{I_B}$$

$$\text{Overdrive factor} = \frac{I_B}{I_{B(EOS)}}$$